

# Boundary-lubricated friction in presence of a nano-well

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**Abstract** The advantage of surface macro- and micro-  
scopic patterning has been recently proved for improving  
tribological performances of mechanical sliding contacts.  
The effects of scaling down the texturing dimensions to the  
nanoscale have not yet been investigated to a comparable  
extent. By means of classical Molecular Dynamics simu-  
lations, we show that the frictional behavior of a thin film  
in boundary-lubricated regime is significantly affected by  
the presence of nanoscale superficial patterning of the  
moving confining walls, leading to a significant suppres-  
sion of the high dissipative stick-slip dynamics and a  
consequent friction reduction. We believe these findings to  
be relevant for nanotechnology applications.

## Introduction

Introduction of specific *micro* textures on sliding surfaces,  
involving flat and smooth regions interrupted by local  
depressions, has turned out to be an efficient approach to  
improve tribological properties of mechanical and tech-  
nological devices. One recognized effectiveness is that of  
trapping wear particles. The elimination of wear debris  
from the matting interface reduces the ploughing

component of friction. Another important role of the sur-  
face local depressions is to act as reservoir for lubricants  
capable of feeding it directly between the two contacting  
surfaces [1, 2].

When a confined lubricant is characterized by a large  
surface-to-volume ratio, the surface properties strongly  
affect its tribological properties. In Ref. [3], it is shown  
how, in presence of patterned surfaces, the concerted effect  
of wetting properties and surface roughness may consid-  
erably reduce friction of a fluid lubricant past the  
boundaries. Under a certain pressure  $P_N$  the micro-  
scopic patterning reduces the wettability of the substrate,  
which is only weakly coupled to the liquid lubricant: momentum  
transfer parallel to the interface is strongly reduced.

If the width of the lubricant is reduced to a few atomic  
layers, e.g., because of the squeezing of the lubricant out of  
the contact region due to high load during starting and  
stopping of interface sliding, the atoms or molecules in the  
lubricant film are ordered into layers parallel to the  
bounding walls. Both numerical simulations [4] and  
experiments [5] generally conclude that the film behaves  
like a solid (at least in the mechanical sense that static  
friction is observed) even at temperatures significantly  
higher than its bulk melting temperature. At low driving  
relative velocity of the confining walls, the motion in such  
a system corresponds to the high dissipative stick-slip  
regime, where a melting-freezing mechanism [4] is  
observed; the film melts during slip and solidifies at stick.

In this article we investigate the effects of nanoscale  
surface patterning on the tribological performances of  
sliding contacts under boundary-lubricated conditions. The  
meso-*scopic* frictional response (of the driven wall) is  
analyzed in terms of the detailed micro-*scopic* dynamics  
and structural transitions of the confined lubricant layers  
under shear.

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From an experimental view point, nanoscale patterns can be suitably created by means of laser surface texturing or by focused ion beam milling.

Recent studies (e.g., the first two cited references) have undoubtedly proved the usefulness of micro-scopic surface patterning for the improvement of mechanical performances of sliding contacts. The effects of scaling down the texturing dimensions to the nanoscale have not yet been investigated to a comparable extent. This is exactly the aim of our theoretical/computational work. A more detailed discussion on experimental surface patterning techniques and applications goes beyond the scopes of our manuscript.

## Model

We are interested in the regime of boundary lubrication, when the sliding surfaces are separated by only a few layers of lubricant atoms or molecules. This investigation has at present been restricted to a two-dimensional system consisting of a rigid, patterned substrate (mimicking the texturing of experimental substrates), a moving rigid flat surface (mimicking the driven top wall) and  $n_l$  lubricant particles sandwiched in between. Even if quite general cases has been considered, our simulation results mainly focus here on the boundary regime where the lubricant forms three embedded layers. Increasing the film width (always remaining in the boundary-lubricated regime), it has been observed [6] that static friction decreases approximately exponentially. In order to account for possible dependence on wetting and contact angle properties, our 2D modeling will properly deserve future extension to three-dimensional simulations.

The driven top plate and the bottom substrate, characterized here by the same lattice constant  $a_s = 1$ , are made up of  $n_t$  and  $n_b$  particles, respectively. We use dimensionless units with top, bottom, and lubricant atoms all having mass  $m = 1$ . The rigid top substrate of mass  $M_{\text{top}} = m n_t$  is pulled through a spring, of elastic constant  $K$ , connected to a stage which moves along the horizontal  $x$  direction with constant velocity  $V_{\text{ext}}$ . A loading force  $L$  is applied to the top plate along the vertical  $y$  direction. Due to the vertical confinement, periodic boundary conditions are applied only along the  $x$  direction. Considering a non-polar lubricant, all atoms interact via a standard 6–12 Lennard–Jones pairwise potential

$$V_{\alpha\alpha'}(r) = V_{\alpha\alpha'} \left[ \left( \frac{r_{\alpha\alpha'}}{r} \right)^{12} - 2 \left( \frac{r_{\alpha\alpha'}}{r} \right)^6 \right] \quad (1)$$

where  $\alpha, \alpha' = \text{l, t, b}$  refer to lubricant, top and bottom particles, respectively. To reduce the number of parameters, we study the tribological response of the system in the perfect commensurate case where  $r_{\text{tl}} = r_{\text{tl}} = r_{\text{bl}}$

( $\equiv r_0 = 1$ ), focusing on pairwise potentials having the same interaction strength,  $V_{\text{tl}} = V_{\text{tl}} = V_{\text{bl}}$  ( $\equiv V_0 = 1$ ). This case may correspond to an intermediate physical situation between that of a “soft” and a “hard” lubricant [7]. The cut-off radius for interactions is  $r^* = 2.5 r_0$ . No direct interaction between the top plate and bottom substrate is taken into account. The model is sketched in Fig. 1.

The top plate dynamics satisfies the equations

$$\begin{aligned} M\ddot{X}_{\text{top}} + \sum_{i=1}^{n_l} \sum_{j=1}^{n_l} \frac{d}{dx_{jt}} V_{i,l}(|r_{il} - r_{jl}|) + K(X_{\text{top}} - V_{\text{ext}}t) &= 0, \\ M\ddot{Y}_{\text{top}} + \sum_{i=1}^{n_l} \sum_{j=1}^{n_l} \frac{d}{dy_{jt}} V_{i,l}(|r_{il} - r_{jl}|) + L &= 0, \end{aligned} \quad (2)$$

where  $X_{\text{top}}$  and  $Y_{\text{top}}$  stand for its center of mass coordinates. The equations of motion for the displacement vectors  $\mathbf{r}_{il}$  of the  $n_l$  lubricant atoms are given by

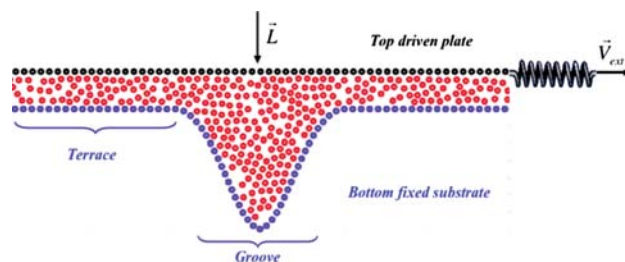
$$\begin{aligned} m\ddot{u}_i + \frac{d}{du_i} \sum_{i \neq j}^{n_l} V_{i,l}(|r_{il} - r_{jl}|) \\ + \sum_{\beta=\text{t,b}} \frac{d}{du_i} \left[ \sum_i^{n_l} \sum_j^{n_\beta} V_{\beta,l}(|r_{i\beta} - r_{j\beta}|) \right] + \text{N.H.C.} \\ = 0, \end{aligned} \quad (3)$$

where  $u_i = x_{il}$  or  $y_{il}$ . The temperature control of the system is achieved by means of a Nose'-Hoover chain of thermostats (NHC) acting on the lubricant particles. The coupled equations of motion (2–3) are integrated using the standard fourth-order Runge–Kutta algorithm.

All units are expressed in LJ units  $V_0, r_0$  and the masses of the individual atoms  $m_0$ . Taking as an example the interaction parameters between two Xe atoms:  $V_0 = 19.83$  meV,  $r_0 = 4.055$  Å and  $m_0 = 2.16 \times 10^{-22}$  g, e.g., the time unit becomes

$$t_0 = (m_0 r_0^2 / V_0)^{1/2} = 3.345 \text{ ps}$$

The shape of the pattern groove in the bottom substrate is modeled by means of the Peyrard and Remoissenet potential [8]



**Fig. 1** Sketch of the system. The lubricant is confined between the top driven plate and the patterned substrate. Here the horizontal dimension of the system is 60 (L-J units)

$$V_{\text{sub}}(x) = A \frac{(1+s)^2(1-\cos x)}{1+s^2-2s\cos x}, |s| < 1, \tag{4}$$

which has proven to be an efficient on-site potential for describing many realistic situations. The parameter  $s$  characterizes the shape of the groove, ranging from spiky narrow dimple to flat large pattern; the parameter  $A$  varies the depth. While in the present paper we focus on a fixed choice of the parameter ( $s = 0.1$ ), future investigations will be devoted to a detailed study of the influence of the groove shape on sliding friction.

At the beginning of the simulation procedure, the groove is empty and the particles, confined between top plate and bottom substrate, are ordered in layers and placed at a uniform separation. Due to the applied load  $L$ , the lubricant particles start to fill up the available empty space. After a transient time interval  $\Delta t_1$ , the groove turns out to be almost completely filled, and the oscillations of the top plate decrease considerably. Figure 1 shows a typical spatial configuration of the lubricant particles after this system relaxation. Then, the stage attached to the top plate via the spring  $K$  starts moving at the constant velocity  $V_{\text{ext}}$ . A time interval  $\Delta t_2$  is necessary to reach a steady state dynamics where the bottom groove is filled and three fully discernible layers form between the top plate and the bottom terraces. It is important to note that the number of lubricant particles has been carefully chosen in such a way that the groove fills up and a three layer film is formed with particles uniformly distributed and no intrinsic defects:  $n_1$  has been actually taken as the largest number for which the film thickness (between the top plate and the bottom terraces) remains equal to three full layers, the addition of extra particles resulting in an unstable situation with thickness irregularly oscillating between three and four layers. At this point, we start calculating and recording the system characteristics of relevant physical interest. In our system the external spring elongation ( $X_{\text{top}}(t) - V_{\text{ext}} t$ ) gives a direct measure of the *friction force* experienced by the system. The average friction ( $av\_fric$ )

$$av\_fric = K_{\text{ext}} \langle X_{\text{top}}(t) - V_{\text{ext}} t \rangle \tag{5}$$

is evaluated as the *friction force* averaged over a long enough time interval during the steady sliding state of the system.

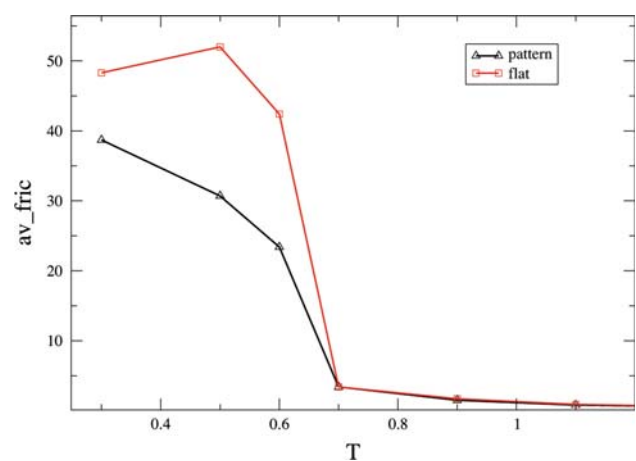
In this work we focus on the case of commensurability among the three inherent system “lengths”  $r_{1l}$ ,  $r_{1t}$ ,  $r_{1b}$ . Experimentally, commensurability is not a common situation and can only be achieved under well-controlled operating conditions [9]. However our situation could represent the physical situation in which, two lubricant layers stick to the confining substrate walls and become “rigid”: our rigid substrates would be the lubricant layer stuck on a second rigid (and not necessarily commensurate)

substrate. Commensurability means optimal structural match between the crystalline lubricant and the wall. This feature enhances the ordering tendency, which also results from entropy reduction of the disordered molecules near the walls [10]. In our case this increased ordering tendency competes with the disorder effect due to the presence of grooves.

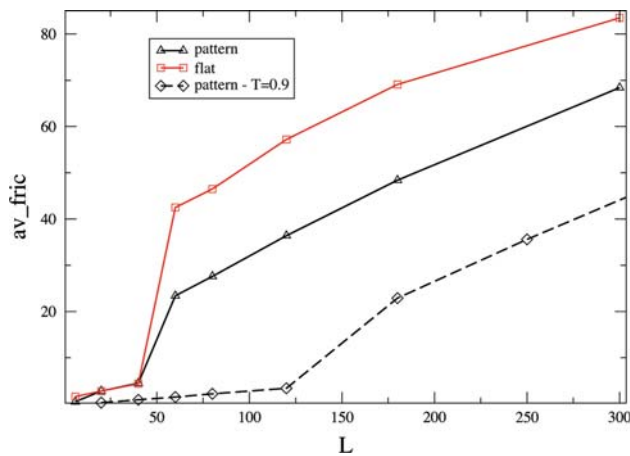
### Results

We checked the system response varying two main parameters: the loading force  $L$ , and the temperature  $T$ . This required to perform a large number of runs with a small time step suitable for atomistic calculations and consequently long simulation times. We found that for a large range of parameters there was a drastic reduction of friction.

However the patterning strongly reduces the friction only when the lubricant does not behave ‘liquid-like’. In Fig. 2 a threshold  $T_{\text{thr}}$  ( $=0.7$ ) appears: looking at the lubricant ‘*radial distribution function*’ for temperatures above  $T_{\text{thr}}$ , it turns out that the lubricant is liquid-like and the patterning does not affect significantly the tribological behavior of the system. In this boundary-lubrication regime, viscosity is not supposed to affect much the tribological properties, where the direct interaction between the solid confining surfaces and the lubrication molecules is the crucial factor [4]. While for temperatures under  $T_{\text{thr}}$  the system is in the so-called high dissipative stick-slip regime: the patterning strongly reduces  $av\_fric$ . The trend of  $av\_fric$  clearly shows a threshold  $L_{\text{thr}}$  ( $=40$ ) (Fig. 3) also as a function of the external applied load, where we



**Fig. 2** Average friction as a function of temperature in the case of a flat (*squares*) and a patterned (*triangles*) substrate. There is a sensible reduction of the average friction only under the threshold temperature  $T = 0.7$ . For higher temperatures, the lubricant is liquid. Here  $L = 60$ ,  $V_{\text{ext}} = 0.1$  (L-J units)



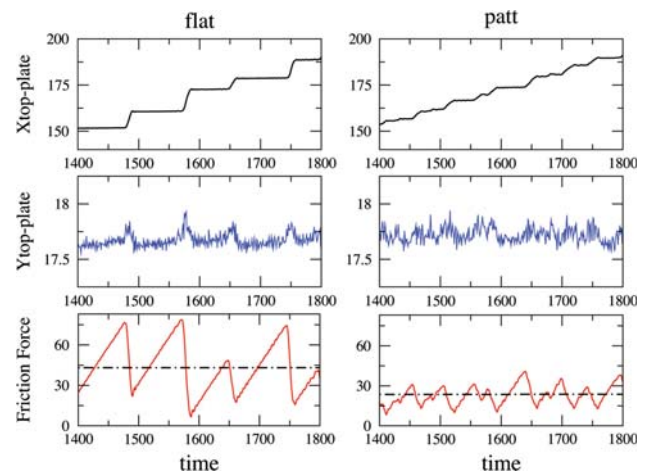
**Fig. 3** Average friction as a function of load in the case of a flat (*squares*) and a patterned (*triangles*) substrate. There is a sensible reduction of the average friction above the threshold  $L = 40$ . For lower loads, the lubricant is liquid. Here  $T = 0.6$ ,  $V_{\text{ext}} = 0.1$  (L-J units). The dashed line is (as before) the average friction versus  $L$  in the patterned case, but at  $T = 0.9$

find a liquid-like behavior and smooth sliding for loads lower than  $L_{\text{thr}}$ , while a stick-slip regime is observed above  $L_{\text{thr}}$ ; in the latter case, the pressure is sufficient to induce a solid-like phase in the lubricant due to the vertical confinement. Fixing a higher value of temperature, and plotting  $av\_fric$  as a function of the applied load, we only see (as we could expect) an increase of the threshold load (Fig. 3).

In the case of boundary-lubricating regime, we have observed the occurrence of the stick-slip dynamics for a large range of external driving velocities: the faster is the stage velocity, the smaller is the stick-slip period. In order to investigate the effectiveness of the surface patterning, in terms of friction reduction, on high dissipative sliding regimes, we focused on the behavior of the system for such a velocity  $V_{\text{ext}}$  that the stick-slip is not suppressed and its time periodicity is sufficiently short. In this way the *friction force* can be correctly averaged on the time interval accessible by the simulation.

Besides in a large range of parameters, for suitable applied loads and temperatures, there is a drastic reduction of friction as shown in Fig. 4. The curves represent the values of the  $x$  and  $y$  coordinates of the top plate and the *friction force* as a function of time in the flat and patterned case. The  $x$  coordinate of the top plate clearly shows a step-like behavior: in the stick phase (flat regions) the external work is accumulated in potential energy of the spring while in the slip phase this energy is converted in kinetic energy of the moving top plate.

In correspondence of each ‘slip’, the top plate goes up ( $y$  coordinate) and quickly comes down (in order to overcome the potential barrier due to the geometrical interlocking



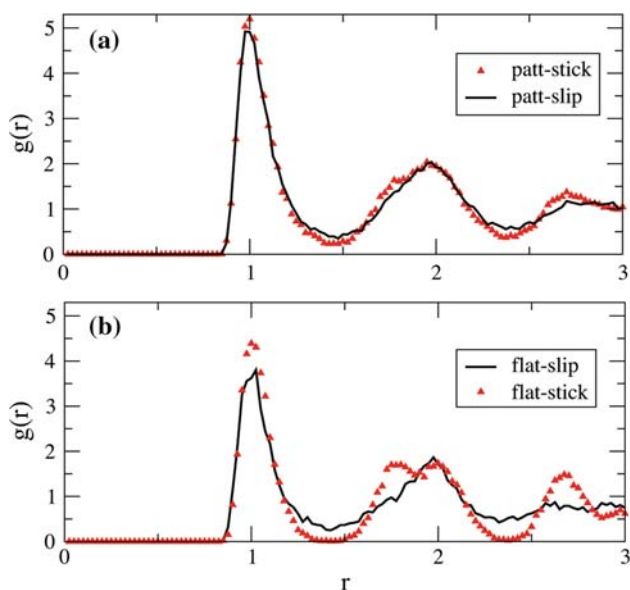
**Fig. 4** Comparison between the stick-slip behavior in the case of flat substrate (*left panels*) and patterned substrate (*right panels*). The dashed line represents  $av\_fric$  (average friction). Here  $nl = 290$  and  $180$ , in the patterned and the flat case,  $T = 0.6$ ,  $k = 7$ ,  $V_{\text{ext}} = 0.1$  (L-J units)

between the rigid top plate and the solid lubricant). The main effect of patterning is the mitigation of the stick-slip regime with a consequent reduction of friction.

Now we want to understand which is the state of the lubricant in the “*reduced-friction*” regime (for suitable applied  $L$ ,  $T$ , and  $V_{\text{ext}}$ ). The answer is not easy because our system shows an alternation of a static (stick) and dynamical (slip) phase. Then we must distinguish between the stick and slip phase. In the flat case the  $g(r)$  calculation shows a clear peaks structure in the stick phase (characteristic of an hexagonal structure), and a more liquid-like structure in the slip phase (Fig. 5b). This is not surprising and is related to the well-known stick-slip melting-freezing mechanism often reported in literature [4]. Moreover, in the case of a patterned substrate, we never find a solid-like structure neither in the stick nor in the slip phase (Fig. 5a): the difference between the stick and slip phase is not so evident. We can only state that the lubricant is more ordered in the stick phase with respect to the slip phase.

In literature the confinement-induced liquid–solid transitions are well known. By reducing the distance between two confining flat walls to few atomic lubricant layers it is possible to induce a layering and often a solidification: the confinement decreases the entropy of the film and shifts the bulk melting transition to higher temperatures and lower pressure. In our system we could expect a solid phase nearby the terraces and a liquid one in the groove, where the lubricant particles are far apart from the substrates. In Ref. [10] a system of molecules confined between two smooth walls is studied by means of a mean-field theory for confinement-induced phase transition, based on a Ginzburg-Landau expression for the free energy. They show the existence of a *surface-ordered* phase in presence of a

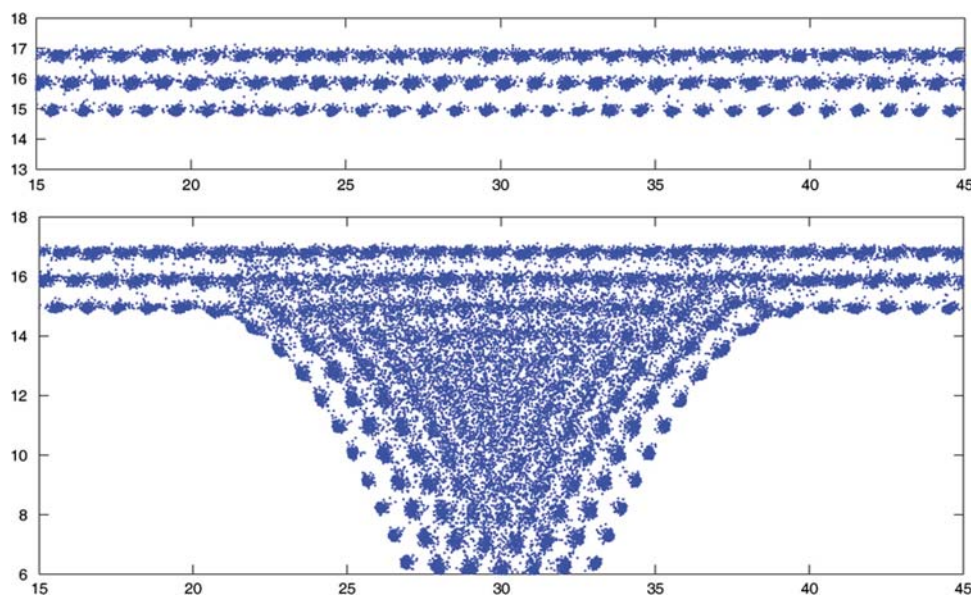




**Fig. 5** Radial distribution function calculation  $g(r)$  (a)  $g(r)$  calculation in the case of patterned substrate in the stick (red triangles) and slip (solid line) phase. (b)  $g(r)$  calculation in the case of a flat substrate in the stick (red triangles) and slip (solid line) phase. In the stick phase the peaks are the typical one of an hexagonal structure

“large enough reduction of the surface free energy achieved by surface ordering”. In this case the phase diagram includes an additional region in which the layers adjacent to the walls are crystalline but at the center the ordering almost vanishes. In our case we think that structural match, due to the perfect commensurability between the solid lubricant lattice constant and the one of substrate, enhances the surface ordering tendency. So our system could stay in the *surface-ordered* phase, which is not a fully crystalline phase. The little diffusive tendency, also

**Fig. 6** Trajectories of all lubricant particles for a time interval  $\Delta t = 200$ . (Top) Flat substrate. (Down) Patterned substrate. The destruction of the hexagonal structure at the center of the groove is clearly visible. The points between layers indicate that the particles pass from a layer to another: the diffusion is increased, especially on the left of the pattern. Here  $T = 0.6$ ,  $V_{ext} = 0.1$ ,  $L = 60$  (L-J units)



visible in the flat case (Fig. 6), supports this hypothesis. But this is not surprising: some experimental studies [11] also conclude that the confinement-induced “solidification” does not consist of a well-definite crystallized structure. The patterning destroys the horizontal ordering generated by the flat walls and induces a melting nearby the grooves. Figure 6 reports the trajectories of all lubricant particles in a time interval  $\Delta t = 200$  in the flat case and in the patterned case.

The figures show how the lubricant dynamics is influenced by patterning also where the particles are far from the grooves: the diffusion between the three ordered lubricant layers is strongly enhanced, also in correspondence of the terraces (points between layers). This increase is especially visible on the left of the groove. The diffusion zone is slightly shifted in the opposite direction with respect to the direction of motion of the top (right).

### Conclusions and perspectives

The above considerations and results demonstrate that the frictional behavior of a thin lubricant film in boundary-lubricated regime is significantly affected by the presence of nanoscale superficial patterning of the moving confining walls. The main effect of the nano-patterning is the ‘mitigation’ of the high dissipative stick-slip regime and a consequent friction reduction. This mitigation is due to a local melting of the lubricant in correspondence of the grooves and to an increase of the diffusion between the lubricant layers. All our simulation results refer to the same groove geometry ( $width = 20$ ,  $depth = 14$  L-J units).

Some simulations were also devoted to the study of  $av_{fric}$  as a function of the groove depth: we kept the

groove *width* constant and varied the *depth*. Some preliminary results show that there is always a threshold depth: grooves deeper than this threshold do not affect further the tribological response of the lubricant.

Future simulations will be also devoted to the study of  $av_{fric}$  as a function of the density of the grooves, keeping the shape of the grooves fixed and varying the distance between them. Moreover the stick-slip mechanism is typically dependent on the external velocity: the increase of the sliding velocity leads to a disappearance of the stick-slip. We will study  $av_{fric}$  as a function of the external dragging velocity in terms of the detailed micro-scopic dynamics and structural transitions of the confined lubricant.

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